

# PE-GE Model



## **SENSITIVITY ANALYSIS ON ARMINGTON ELASTICITIES**

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# Outline



- **What are Armington elasticities?**
- **Initial experiment undertaken in PE-GE model**
- **1st Extention:**
  - Doubling Armington elasticities in the PE-GE model
- **2nd Extention:**
  - Systematic Sensitivity Analysis (around both the original and doubled values)

# What are Armington elasticities?



- Derived from Paul Armington in “A Theory of Demand for Products Distinguished by Place of Production” (1969)
- Give the degree of substitution between imported and domestic goods
- Estimated from econometric analysis

# Initial experiment undertaken in PE-GE model



- **PE-GE model focuses on automobile in India such as:**
  - Aggregated auto sector in GE model
  - Disaggregated into 5 industries (i.e. Motorcycles, Motorcycles parts, Automobiles, Engine parts and Other transport) in PE model
- **Initial simulation:**
  - Multilateral\* full trade liberalization in the 5 automobile industries

*(\*all 3 regions of the model fully liberalize)*

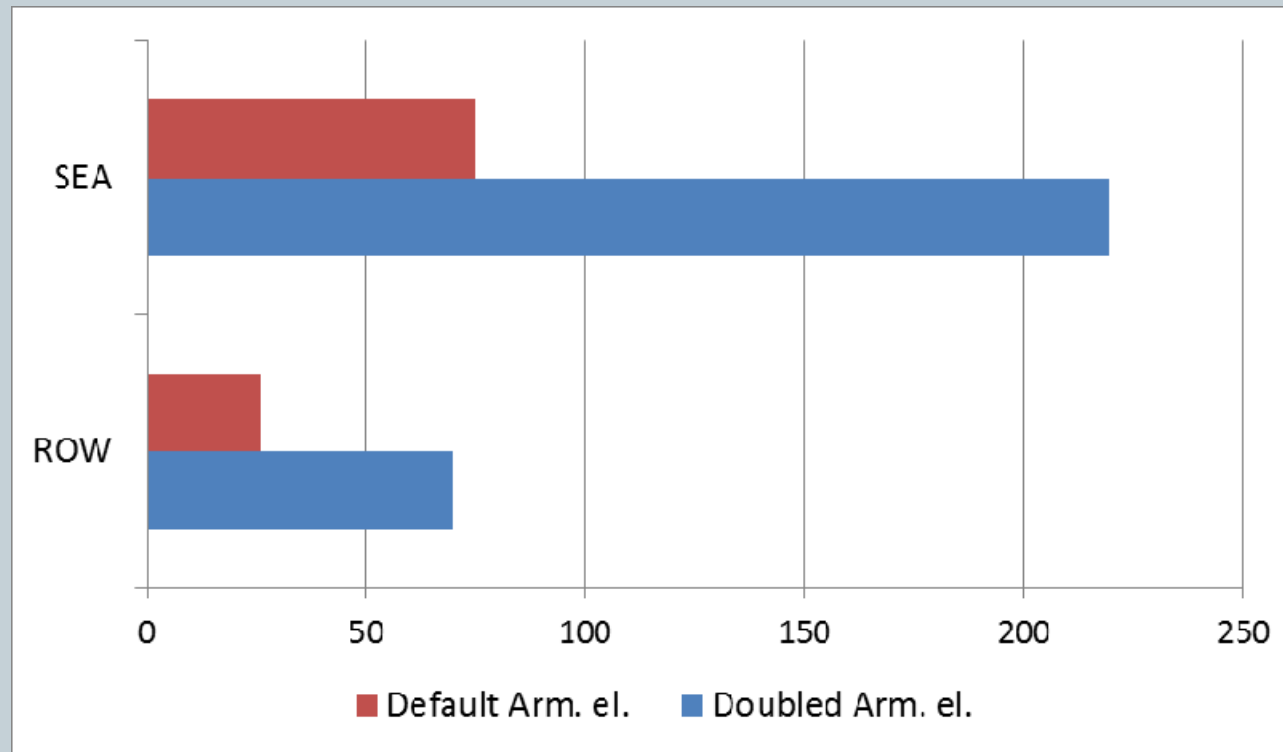
# 1st Extension: Doubling Armington elasticities in PE-GE model - Shocks



- Corresponding parameters and default values in PE-GE model:
  - Elasticities of substitution between domestic and imports of disaggregated industries:  $ESUBDK(k) = 3,2$
  - Elasticities of substitution among imports of disaggregated industries in Armington structure:  $ESUBMK(k) = 6,4$
- Shocks to be implemented – Doubling above values of elasticities such as:
  - $ESUBDK(k) = 6,4$
  - $ESUBMK(k) = 12,8$

# 1st Extension: Doubling Armington elasticities in PE-GE model – Key results

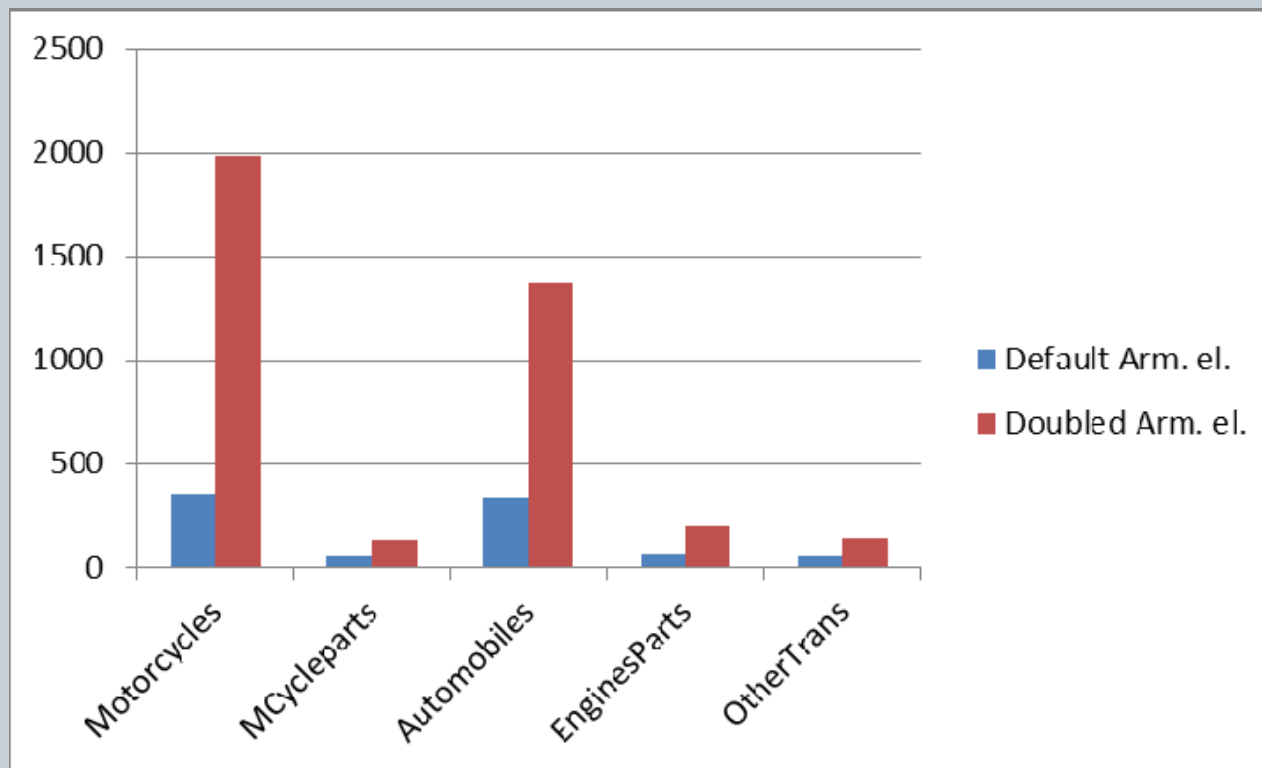
- Changes in India's aggregated auto industry imports from SouthEast Asia (SEA) and Rest of the World (ROW) following multilateral full trade lib'n - Default vs. Doubled Arm. el. - %



*Source: Authors' calculations based on GTAP model*

# 1st Extension: Doubling Armington elasticities in PE-GE model – Key results

- Changes in India's disaggregated auto industry imports from SouthEast Asia (SEA) following multilateral full trade lib'n - Default vs. Doubled Arm. el. - %



*Source: Authors' calculations based on GTAP model*

# 1st Extension: Doubling Armington elasticities in PE-GE model – Key results



- Changes in India's welfare (decomposition) - %

	Total welfare	Allocation efficiency	Terms of Trade	Investment-Savings
Default Arm. el.	57,2	67,2	-20,0	9,9
Doubled Arm. el.	327,5	260,9	36,8	29,8

*Source: Authors' calculations based on GTAP model*

- *Thanks to doubled Armington elasticities, India's terms of trade even become positive (Indian consumers paying less for imported goods; decomposition of terms of trade indicates that most of the ToT gains come from a fall in import price of engine parts)*



## 2nd Extension: Systematic Sensitivity Analysis



### Two Sensitivity analyses

- SSA around original elasticities

$$ESUBDK(k) = 3,2$$

$$ESUBMK(k) = 6,4$$

- SSA around double original elasticities

$$ESUBDK(k) = 6,4$$

$$ESUBMK(k) = 12,8$$

- $ESUBDK(k)$  = Elasticities of substitution between domestic and imports of disaggregated industries
- $ESUBMK(k)$  = Elasticities of substitution among imports of disaggregated industries in Armington structure

## 2nd Extension: Systematic Sensitivity Analysis



### Sensitivity analyses

- $ESUBDK(k) \pm 50\% \text{ \& } ESUBMK(k) \pm 50\%$
- $2*ESUBDK(k) \pm 50\% \text{ \& } 2*ESUBMK(k) \pm 50\%$
- $2*ESUBDK(k) \pm 25\% \text{ \& } 2*ESUBMK(k) \pm 25\%$

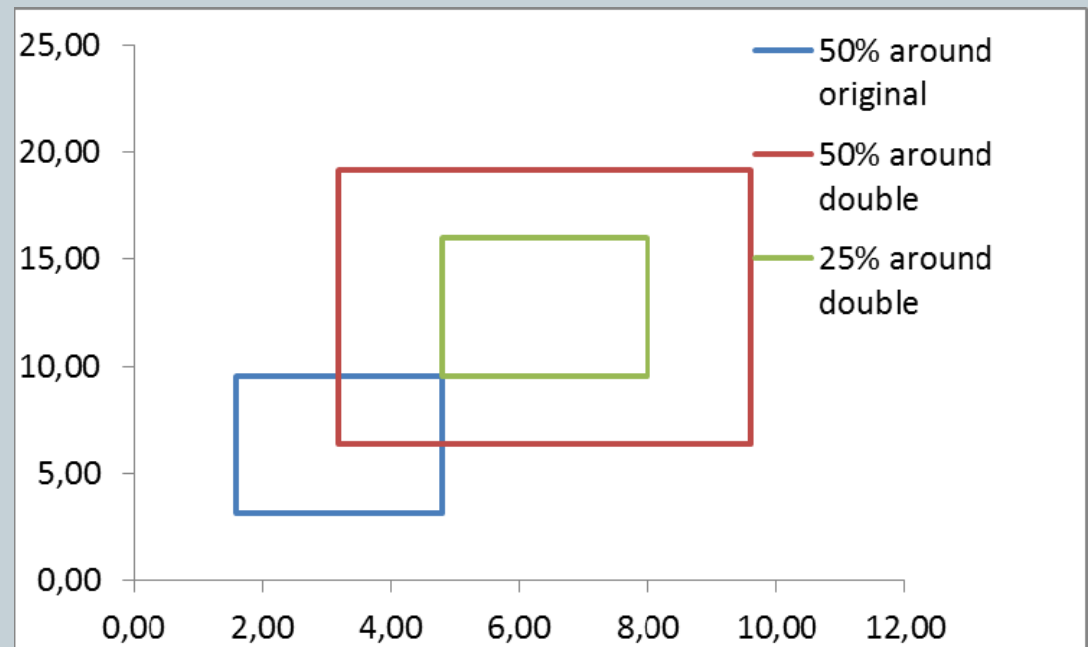
# 2nd Extension: Systematic Sensitivity Analysis

Upper and lower bounds of each variable

Chebyshev's inequality:

The probability that the value of Y lies within k standard deviations of the mean is no less than  $1 - 1/(k^2)$ , which is 0.95 for  $k = \sqrt{20}$

Upper Bound	$M + k \cdot SD$
mean	M
Lower Bound	$M - k \cdot SD$
standard dev.	SD



## 2nd Extension: Systematic Sensitivity Analysis

- *SSA around original 50%*

qimk[*INDIA]	1 Motorcycle	2 MCyclepar	3 Automobi	4 EnginesPa	5 OtherTrans
Upper Bound	918,60	107,19	394,17	123,82	50,09
mean	342,19	54,06	167,70	58,48	24,51
Lower Bound	<b>-234,22</b>	0,93	<b>-58,77</b>	<b>-6,86</b>	<b>-1,07</b>
standard dev.	128,89	11,88	50,64	14,61	5,72

- *SSA around double 50%*

qimk[*INDIA]	1 Motorcycle	2 MCyclepar	3 Automobi	4 EnginesPa	5 OtherTrans
Upper Bound	6763,97	251,60	1550,58	341,14	132,08
mean	2002,62	130,41	607,90	156,71	66,52
Lower Bound	<b>-2758,73</b>	9,22	<b>-334,78</b>	<b>-27,72</b>	0,96
standard dev.	1064,67	27,10	210,79	41,24	14,66

## 2nd Extension: Systematic Sensitivity Analysis

- *SSA around original*

<b>pimk[*INDIA]</b>	1 Motorcycle	2 MCyclepar	3 Automobi	4 EnginesPa	5 OtherTrans
Upper Bound	-36,68	-16,24	-27,72	-15,93	-8,54
mean	-36,86	-16,60	-27,99	-16,11	-8,67
Lower Bound	-37,04	-16,96	-28,26	-16,29	-8,80
standard dev.	0,04	0,08	0,06	0,04	0,03

- *SSA around double*

<b>pimk[*INDIA]</b>	1 Motorcycle	2 MCyclepar	3 Automobi	4 EnginesPa	5 OtherTrans
Upper Bound	-36,77	-15,65	-27,96	-16,00	-8,62
mean	-37,04	-16,32	-28,09	-16,36	-8,84
Lower Bound	-37,31	-16,99	-28,22	-16,72	-9,06
standard dev.	0,06	0,15	0,03	0,08	0,05

# 2nd Extension: Systematic Sensitivity Analysis

- *SSA around original 50%*

qxsk[**INDIA]	1 SEAsiaOther				
	1 Motorcycles	2 MCycleparts	3 Automobile	4 EnginesPar	5 OtherTrans
Upper Bound	987,95	109,20	769,87	147,18	99,04
mean	378,31	55,49	349,80	73,03	55,35
Lower Bound	-231,33	1,78	-70,27	-1,12	11,66
standard dev.	136,32	12,01	93,93	16,58	9,77
	3 ROW				
	1 Motorcycles	2 MCycleparts	3 Automobile	4 EnginesPar	5 OtherTrans
Upper Bound	631,48	74,67	297,60	91,44	41,50
mean	210,43	28,25	113,12	35,00	16,68
Lower Bound	-210,62	-18,17	-71,36	-21,44	-8,14
standard dev.	94,15	10,38	41,25	12,62	5,55

# 2nd Extension: Systematic Sensitivity Analysis

- *SSA around double 50%*

qxsk[**INDIA]	1 SEAsiaOther				
	1 Motorcycles	2 MCycleparts	3 Automobile	4 EnginesPar	5 OtherTrans
Upper Bound	7602,21	257,19	3498,80	436,81	280,91
mean	2269,28	133,85	1400,29	205,65	149,97
Lower Bound	-3063,65	10,51	-698,22	-25,51	19,03
standard dev.	1192,48	27,58	469,24	51,69	29,28
	3 ROW				
	1 Motorcycles	2 MCycleparts	3 Automobile	4 EnginesPar	5 OtherTrans
Upper Bound	3916,88	154,39	1027,82	206,14	104,36
mean	1079,89	67,90	363,84	77,83	45,28
Lower Bound	-1757,10	-18,59	-300,14	-50,48	-13,80
standard dev.	634,37	19,34	148,47	28,69	13,21

## 2nd Extension: Systematic Sensitivity Analysis

- *SSA around original*

qdmk[*INDIA	1 Motorcycle	2 MCyclepai	3 Automobi	4 EnginesPa	5 OtherTrans
Upper Bound	1,31	0,69	0,87	-1,16	-1,27
mean	-1,33	-10,58	-6,55	-7,06	-5,21
Lower Bound	-3,97	-21,85	-13,97	-12,96	-9,15
standard dev.	0,59	2,52	1,66	1,32	0,88

- *SSA around double*

qdmk[*INDIA	1 Motorcycle	2 MCyclepai	3 Automobi	4 EnginesPa	5 OtherTrans
Upper Bound	14,42	8,60	15,18	6,00	6,18
mean	5,16	-17,38	-14,92	-10,19	-4,33
Lower Bound	-4,10	-43,36	-45,02	-26,38	-14,84
standard dev.	2,07	5,81	6,73	3,62	2,35



## 2nd Extension: Systematic Sensitivity Analysis

- *SSA around original 50%*

qimk[*INDIA]	1 Motorcycle	2 MCyclepar	3 Automobi	4 EnginesPa	5 OtherTrans
Upper Bound	918,60	107,19	394,17	123,82	50,09
mean	342,19	54,06	167,70	58,48	24,51
Lower Bound	<b>-234,22</b>	0,93	<b>-58,77</b>	<b>-6,86</b>	<b>-1,07</b>
standard dev.	128,89	11,88	50,64	14,61	5,72

- *SSA around double 25%*

qimk[*INDIA]	1 Motorcycle	2 MCyclepar	3 Automobi	4 EnginesPa	5 OtherTrans
Upper Bound	4076,43	190,76	1050,81	247,16	98,71
mean	1810,49	130,03	594,43	154,99	66,02
Lower Bound	<b>-455,45</b>	69,30	138,05	62,82	33,33
standard dev.	506,68	13,58	102,05	20,61	7,31

## 2nd Extension: Systematic Sensitivity Analysis

- *SSA around original 50%*

<b>pimk[*INDIA]</b>	1 Motorcycle	2 MCyclepar	3 Automobi	4 EnginesPa	5 OtherTrans
Upper Bound	-36,68	-16,24	-27,72	-15,93	-8,54
mean	-36,86	-16,60	-27,99	-16,11	-8,67
Lower Bound	-37,04	-16,96	-28,26	-16,29	-8,80
standard dev.	0,04	0,08	0,06	0,04	0,03

- *SSA around double 25%*

<b>pimk[*INDIA]</b>	1 Motorcycle	2 MCyclepar	3 Automobi	4 EnginesPa	5 OtherTrans
Upper Bound	-36,91	-15,96	-28,05	-16,18	-8,71
mean	-37,04	-16,32	-28,09	-16,36	-8,84
Lower Bound	-37,17	-16,68	-28,13	-16,54	-8,97
standard dev.	0,03	0,08	0,01	0,04	0,03

## 2nd Extension: Systematic Sensitivity Analysis

- *SSA around double 25%*

qxsk[**INDIA]	1 SEAsiaOther				
	1 Motorcycles	2 MCycleparts	3 Automobile	4 EnginesPar	5 OtherTrans
Upper Bound	4598,22	195,31	2425,89	319,07	214,08
mean	2057,96	133,51	1377,53	203,64	149,06
Lower Bound	<b>-482,30</b>	71,71	329,17	88,21	84,04
standard dev.	568,02	13,82	234,42	25,81	14,54
	3 ROW				
	1 Motorcycles	2 MCycleparts	3 Automobile	4 EnginesPar	5 OtherTrans
Upper Bound	2278,86	109,63	681,95	140,30	74,47
mean	953,14	66,65	350,39	76,57	44,91
Lower Bound	<b>-372,58</b>	23,67	18,83	12,84	15,35
standard dev.	296,44	9,61	74,14	14,25	6,61

## 2nd Extension: Systematic Sensitivity Analysis

- *SSA around original 50%*

qdmk[*INDIA	1 Motorcycle	2 MCyclepar	3 Automobi	4 EnginesPa	5 OtherTrans
Upper Bound	1,31	0,69	0,87	-1,16	-1,27
mean	-1,33	-10,58	-6,55	-7,06	-5,21
Lower Bound	-3,97	-21,85	-13,97	-12,96	-9,15
standard dev.	0,59	2,52	1,66	1,32	0,88

- *SSA around double 25%*

qdmk[*INDIA	1 Motorcycle	2 MCyclepar	3 Automobi	4 EnginesPa	5 OtherTrans
Upper Bound	9,70	-4,50	0,87	-2,09	0,89
mean	5,09	-17,51	-14,69	-10,18	-4,43
Lower Bound	0,48	-30,52	-30,25	-18,27	-9,75
standard dev.	1,03	2,91	3,48	1,81	1,19



**Thank you**